



Recursion

Logic Algorithm

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Subject:

1. Overview Recursion
2. Flowchart and pseudocode



Objectives:

1. Students able to understand the underlying concept of Recursion
2. Students able to use flowchart and pseudocode to implement Recursion



Overview

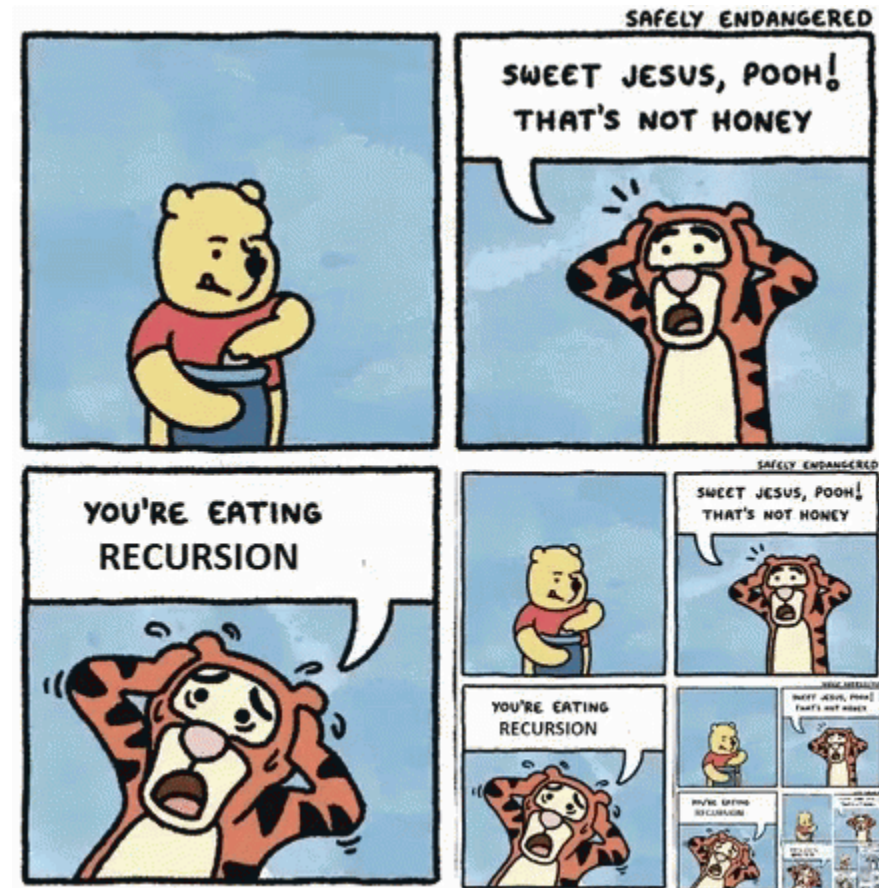
Recursion

- In computer science, recursion is a way of thinking about and solving problems
- It's actually one of the central ideas of CS
- In recursion, the solution depends on solutions to smaller instances of the same problem
- Recursive function is a special type of function which calls itself and repeats its behavior until some condition is met to return a result.



Recursive solutions

- When creating a recursive solution, there are a few things we want to keep in mind:
 - We need to break the problem into smaller pieces of itself
 - We need to define a “base case” to stop recursion
 - The smaller problems we break down into need to eventually reach the base case



Example

```
def compute(Input):  
    if Input <= 2:  
        return Input
```

```
    else:
```

```
        return Input + compute(Input-1)
```

```
def main():  
    print(compute(10))
```

```
main()
```

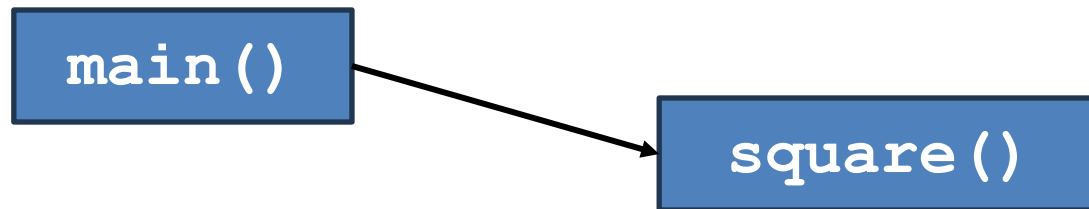
This is called a base case or base condition. If this condition is met, the recursion will stop.

You can see that the `compute()` function calls itself.

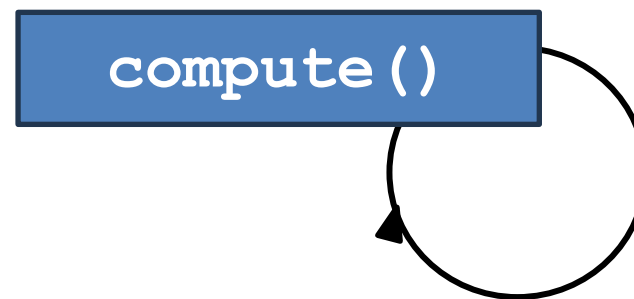
This is where the recursion occurs.

Normal vs Recursive Functions

- So far, we've had functions call other functions
- For example, `main()` function calls the `square()` function



- A recursive function, however, `compute()` function calls itself

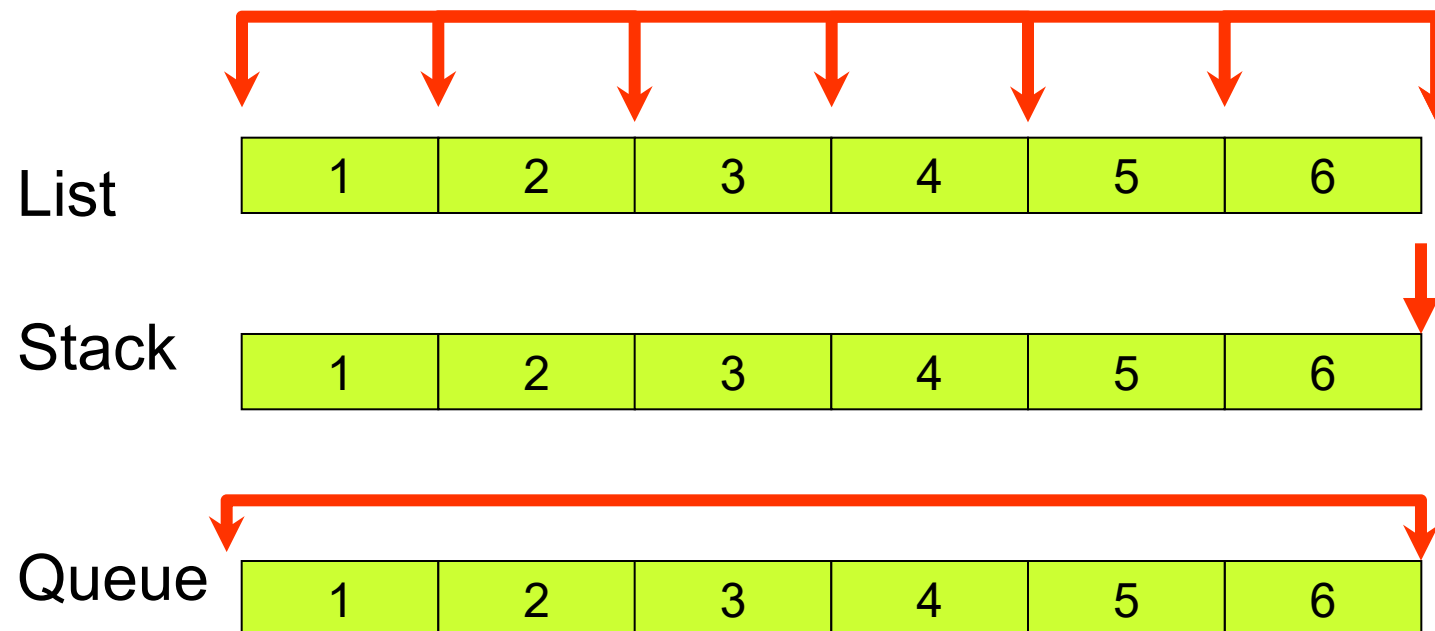


Visualizing Recursion

- To help visualize recursion, we will use a common concept called the Stack and Queue
- Stack – a container that allows push (to put item into stack) and pop (to obtain and remove item from stack)
- Queue – a container that allows enqueue (to put item into queue) and dequeue (to obtain and remove item from queue)

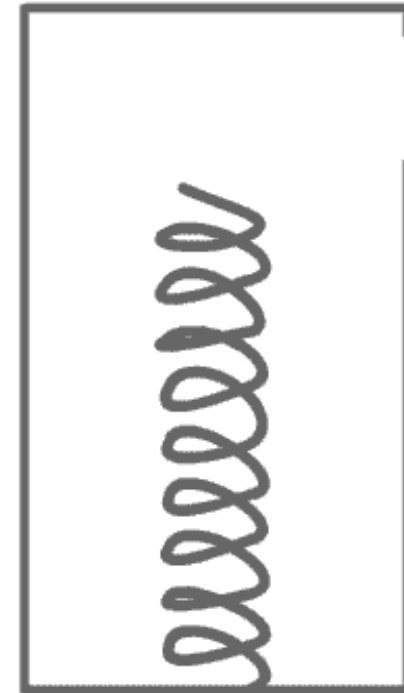
List, Stack and Queue

- In a List, insertion and deletion of elements can be carried out at any position
- However, adding and deleting elements to the stack/queue is done in the leading position or the backward position.



Stack

- Adding and deleting elements is done on the list element located at the front
- Removed element is the most recently added element
- Another name : LIFO (Last In First Out)
- PUSH operation: Adds an element to a stack
- POP operation: Removes an element from a stack



Queue

- Adding data is done at one end of a queue, while deleting data is done at the other end
- Removed data is the earliest data added
- Another name : FIFO (First In First Out)
- ENQUEUE operation: Adds data to a queue
- DEQUEUE operation: Removes data from a queue





Flowchart and Pseudocode

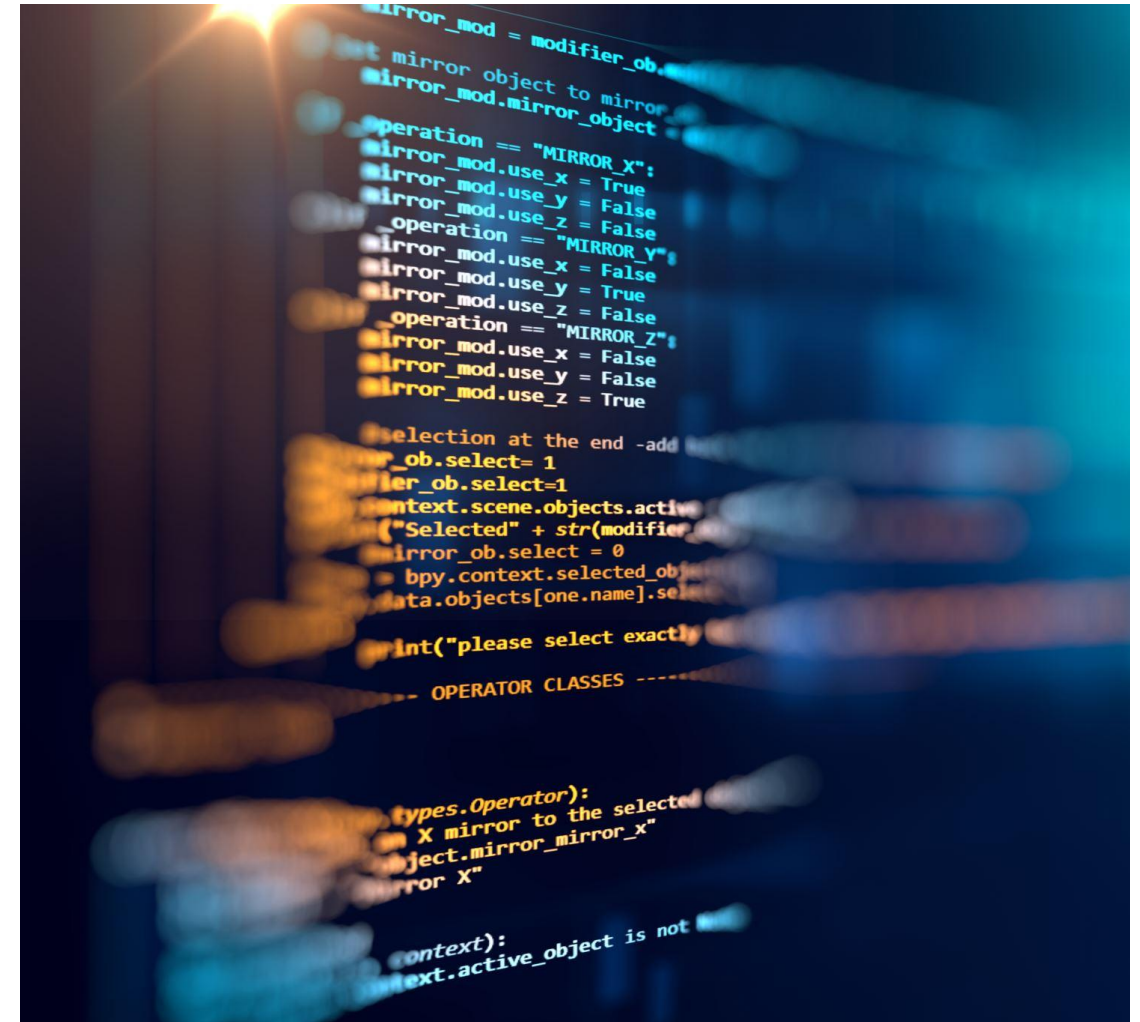
Let's Try

Create program to calculate factorial of a certain number

e.g $4! = 4 \times 3 \times 2 \times 1 = 24$

What is the input, process, and output?

Note: We can use either recursive or non-recursive approach to solve this problem.



Answer (Non-recursive approach)

Create program to calculate factorial of a certain number

e.g $4! = 4 \times 3 \times 2 \times 1 = 24$

What is the input, process, and output?

Input:

Input number (n), set $i = 1$, set $fact = 1$

Process:

for $i = 1$ until n , calculate $fact = fact * i$

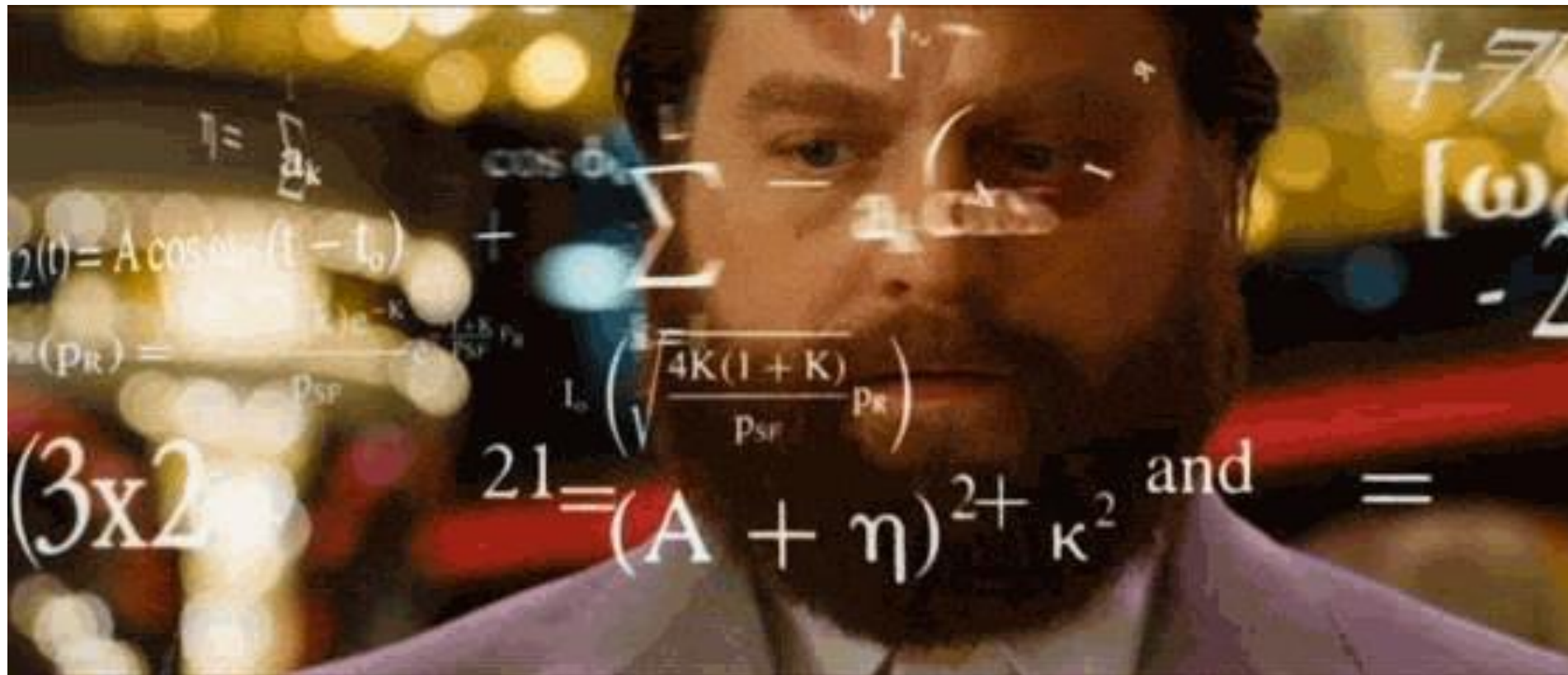
Output:

Display $fact$



Let's Try

Pseudocode ? Flowchart ?

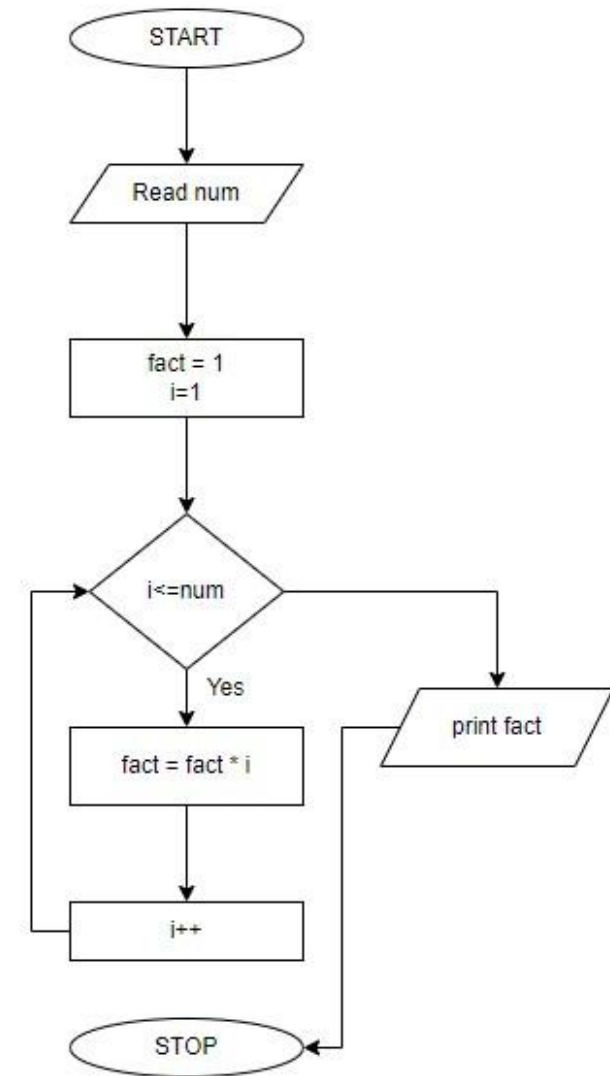


Answer

Pseudocode

1. Start
2. INPUT n
3. SET $i = 1$, $fact = 1$
4. if $i \leq n$ otherwise STEP 6
 Calculate $fact = fact * i$
 $i = i + 1$ back to step 3
5. DISPLAY fact
6. STOP

Flowchart



Answer (Recursive approach)

Create program to calculate factorial of a certain number

1. Break the problem into smaller pieces and look for recurring patterns

<code>factorial(1)</code>	1	1	1
<code>factorial(2)</code>	2 * 1	2 * <code>factorial(1)</code>	2
<code>factorial(3)</code>	3 * 2 * 1	3 * <code>factorial(2)</code>	6
<code>factorial(4)</code>	4 * 3 * 2 * 1	4 * <code>factorial(3)</code>	24

Some of the result of function call (number(s) inside the square box) is replaceable with the result of previous function call

Answer (Recursive approach)

Create program to calculate factorial of a certain number

1. Break the problem into smaller pieces and look for recurring patterns

<code>factorial(1)</code>	1	<code>factorial(1)</code>	1
<code>factorial(2)</code>	$2 * 1$	$2 * \text{factorial}(1)$	2
<code>factorial(3)</code>	$3 * 2 * 1$	$3 * \text{factorial}(2)$	6
<code>factorial(4)</code>	$4 * 3 * 2 * 1$	$4 * \text{factorial}(3)$	24
<code>factorial(n)</code>	$n * (n-1) * (n-2) * \dots * 1$	$n * \text{factorial}(n-1)$	

Answer (Recursive approach)

Create program to calculate factorial of a certain number

2. Define the base case / base condition

<code>factorial(1)</code>	1	1	1
<code>factorial(2)</code>	$2 * 1$	$2 * \text{factorial}(1)$	2
<code>factorial(3)</code>	$3 * 2 * 1$	$3 * \text{factorial}(2)$	6
<code>factorial(4)</code>	$4 * 3 * 2 * 1$	$4 * \text{factorial}(3)$	24

The result of function call is not replaceable with the result of previous function call when input is equal to 1

Answer (Recursive approach)



```
def factorial(x):
```

```
    if x == 1:  
        return 1
```

```
    else:  
        return (x * factorial(x-1))
```

Base case

Recursive case

```
num = 3
```

```
print("The factorial of", num, "is", factorial(num))
```

The factorial of 3 is 6

Answer (Recursive approach)

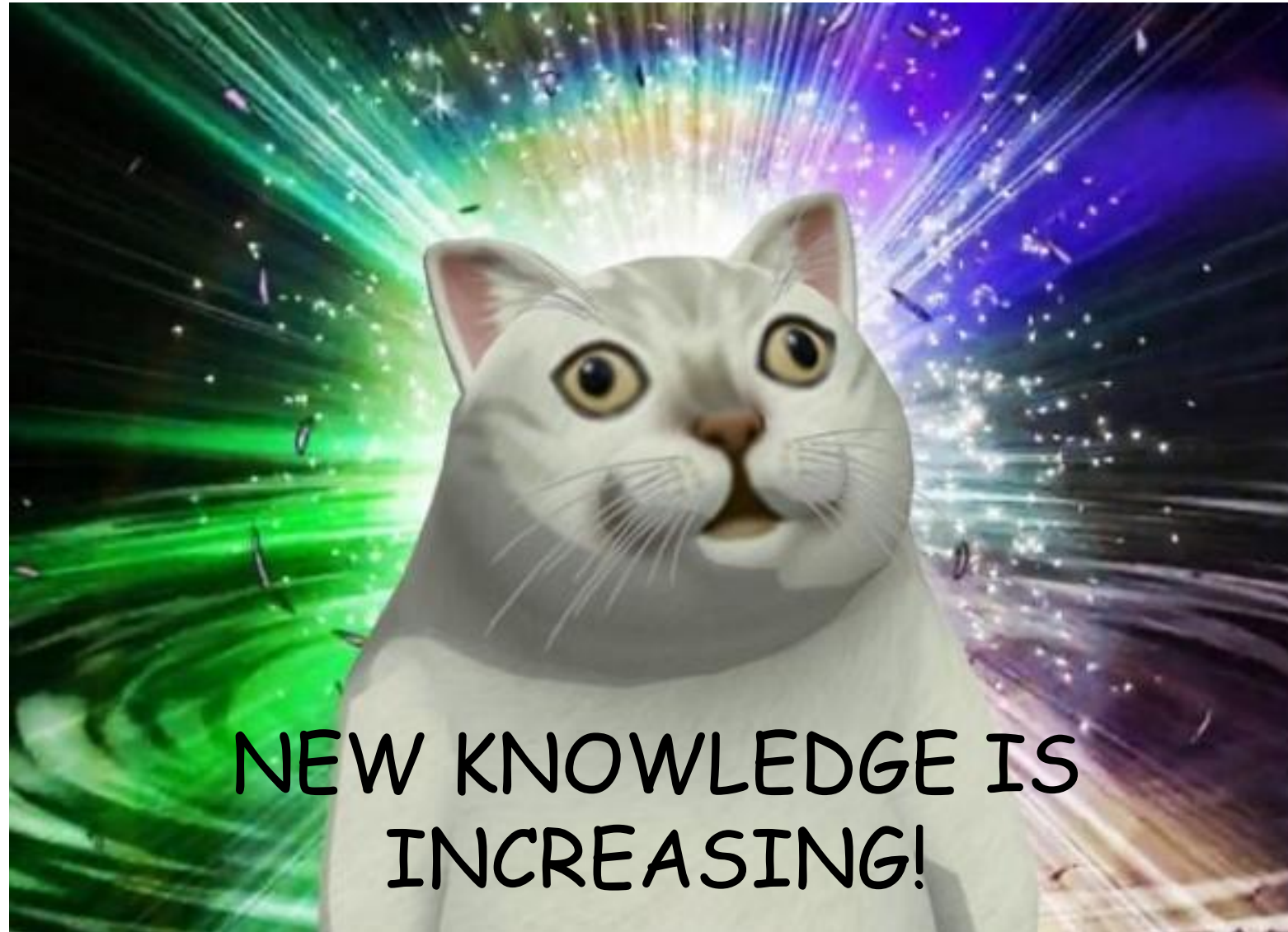
```
▶ def factorial(x):  
    if x == 1:  
        return 1  
    else:  
        return (x * factorial(x-1))  
  
num = 3  
print("The factorial of", num, "is", factorial(num))
```



```
factorial(3)           # 1st call with 3  
3 * factorial(2)       # 2nd call with 2  
3 * 2 * factorial(1)   # 3rd call with 1  
3 * 2 * 1              # return from 3rd call as number=1  
3 * 2                  # return from 2nd call  
6                      # return from 1st call
```

Summary

- Recursion is a way of thinking about and solving problems in which a function calls itself.
- Base case is required for a recursive function to stop calling itself. Without a base case, recursive function will run in an endless loop.



NEW KNOWLEDGE IS
INCREASING!

Reference

1. Karl, Beecher. "Computational Thinking: A Beginner's Guide to Problem-Solving and Programming." Swindon, UK: BCS, The Chartered Institute for IT (2017).
2. CSE 1300 - Introduction to Computing Principles, Kennesaw State University
3. Computer Science (CS) and Computational Thinking (CT) : Pattern Recognition in the AYA curriculum, Miami University

Latihan

Buatlah study kasus sederhana tentang recursive dan jelaskan program dan outputnya?



THANK YOU!